**AIM**- Design and drawing of Cotter Joint

**FUNCTION**- A cotter joint is used to connect one end of a rod is provided with a socket type of end and the other end of the rod is inserted to a socket. The end of the rod which goes into a socket is also called Spigot.

#### **APPLICATIONS-**

- 1. Joints between the piston rod and the cross need of the steam engine.
- 2. Joints between the side spindle and the fork of the valve mechanism.
- 3. Joint between the piston rod and the tail or pump foundation bolts.

#### **ASSUMPTIONS-**

1. The rods are subjected to axial tensile force the effect of steels concentration due to shaft is neglected.

#### **NOTATION-**

F= Axial load carried by the rod

d=Diameter of the rod

d<sub>1</sub>= diameter of spigot

d<sub>2</sub>=diameter of collar

d<sub>3</sub>=outside diameter of sleeve

d<sub>4</sub>=diameter of sleeve or socket

a= width at rod end

b= width of collar

c= width of socket end

e=Thickness of collar

t= thickness of cotter

 $\sigma$ =allowable shear stress

 $\sigma_c$ = allowable crushing stress

### **PROCEDURE:**

**STEP 1:** Design of rods

For the rods under axial load,

Axial stress in the rods,  $\sigma$ = 4F

 $\pi d^2$ 

**STEP 2:** Design of the spigot and the Cotter

- a.) Crushing strength of the cotter,  $F=d_1t\sigma_c$
- b.) Axial stress across the slot of the rod

$$\sigma = \frac{4F}{\pi (d_1)^2 - 4d_1 t}$$

STEP 3: Design of the cotter

Strength of the cotter in double shear  $F = 2bt\tau$ 

STEP 4: Design of the collar

- a.) Bearing stress in the collar,  $\sigma_c = \underline{\qquad 4F} \\ \pi \{ (d_2)^2 (4d_1)^2 \}$
- b.) Shear stress in the collar,  $\tau = \frac{F}{\pi d_1 e}$

# **STEP 5:** Design of the sleeve

a.) Axial stress across the slot of the sleeve

$$\sigma = \frac{4F}{\pi[(d_3)^2-(d_1)^2]-4t(d_3-d_1)}$$

b.) Crushing strength of the socket

$$F = (d_4 - d_1)t \times \sigma_c$$

## STEP 6: Design of the rod end

a.) Shear stress at the rod end due to double shear

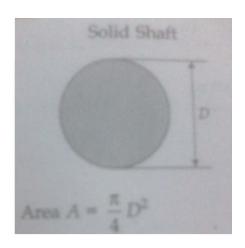
$$\tau$$
=  $\frac{F}{2ad_1}$ 

# STEP 7: Design of the socket end

Shear stress at the socket end, 
$$\tau = \frac{F}{2c(d_4-d_1)}$$

**AIM**-Design of shafts subjected to Torsion, Bending Moment and Combined Bending & Torsion

**INTRODUCTION**- Shaft usually a round member, solid or hollow cross section that rotates and transmits power. It carries machine elements like gears, pulleys, cams, sprockets, couplings etc. Its design primarily consists of finding the size in order to satisfy the strength and rigidity, while transmitting power. Shafts are usually subjected to torsion, bending etc.



#### **NOTATIONS**

P = Power in kW

n= speed in rpm

M<sub>b</sub> = Maximum bending moment on shaft

 $M_t$  = Maximum torque on shaft

D = Diameter of shaft

F = axial or thrust load

K<sub>b</sub> = Combined shock and Endurance factor in Bending

K<sub>t</sub> = Combined shock and Endurance factor in torsion

For rotating shafts with gradually applied loads

$$K_b = 1.5$$
 and  $K_t = 1.0$ 

Suddenly, applied loads with minor shocks,  $K_b = 1.5$  to 2.0 and  $K_t = 1$  to 1.5

Suddenly, applied loads with heavy shocks,  $K_b = 2.0$  to 3.0 and  $K_t = 1.5$  to 3.0

 $\sigma$  = allowable tensile stress for shaft material

 $\tau$  = allowable shear stress for shaft material

### SHAFTS SUBJECTED TO PURE TORSION

Solid Shaft: Diameter of shaft, D = 16K<sub>t</sub> 
$$M_t$$
  $\pi \tau$ 

#### SHAFTS SUBJECTED TO PURE BENDING

Solid Shaft: Diameter of shaft, D = 
$$\frac{32K_bM_b}{\pi\sigma}^{1/3}$$

#### SHAFTS SUBJECTED TO COMBINED BENDING AND TORSION

Solid Shaft:

- i. According to maximum normal stress theory Diameter of Shaft, D =  $\left[\frac{16}{\tau\sigma}\right]$   $\left[K_bM_b + \sqrt{(K_bM_b)^2 + (K_tM_t)^2}\right]^{1/3}$
- ii. According to maximum shear stress theory Diameter of Shaft, D = 1/3 1/3 1/3

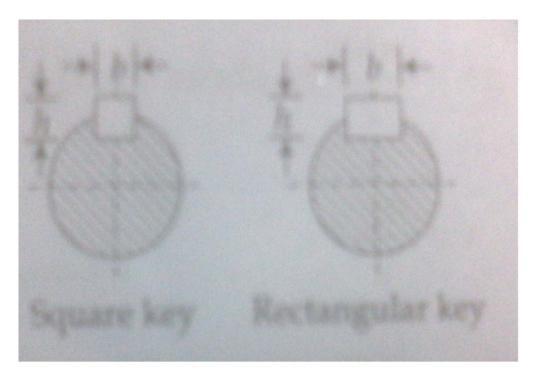
**AIM**- Design of Flat and Square Keys

### **INTRODUCTION**

Keys are used to prevent relative motion between a shaft and the connected member through which torque is being transmitted. Common types of Keys are: Square key, Rectangular key, Feather key, Round key, Gib key, Head key, Taper key, Barth key, Kennedy key, Saddle key and Woodruff key etc.

## **DESIGN OF SQUARE AND FLAT KEY**

The keys are subjected to shear and crushing or bearing stress while transmitting torque.



### **NOTATIONS**

b= width of key

h= thickness

I=length of key

Considering the shearing of key

Shear stress, 
$$\tau = \begin{array}{ccc} F & = & F \\ & Area of shear & bl \end{array}$$

a.) Where F= Force = 
$$\underline{\text{Torque}}$$
 =  $\underline{\text{M}_{\text{t}}}$  =  $\underline{\text{M}_{\text{t}}}$  =  $2\underline{\text{M}_{\text{t}}}$  Radius of shaft r (d/2) d

$$\tau$$
= 2 $M_t$  =>width of the key b = 2 $M_t$  \_\_\_\_ dlb dl $\tau$ 

Considering crushing of key

Crushing stress, 
$$\sigma_c = F = F$$

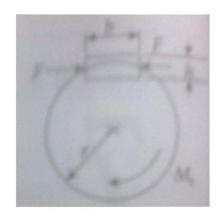
Area of crushing (h/2)I

$$\sigma_c$$
= 2M<sub>t</sub> = 4M<sub>t</sub> => thickness of key h = 4M<sub>t</sub>   
 $\sigma_c$ = d(h/2)I dhldl $\sigma_c$ 

For Square key b=h

$$b = \underbrace{2M_t}_{\text{dh}} \text{ and } \qquad h = b = \underbrace{4M_t}_{\text{dh}}$$

$$M_t = bdl\tau$$
 in shear and  $M_t = bdl\sigma_c$ in crushing  $\frac{}{4}$ 



Procedure Type 1: Length of Key

**STEP 1**: Find Torque, 
$$M_t = \underbrace{9.55 \times 10^6 \text{xP}}_{N}$$
 P=Power in kW, n=speed,rpm

**STEP 2**: Diameter of shaft, d = 
$$\sqrt[3]{\frac{16M_t}{\pi \tau_s}}$$

 $\tau_{\text{s}}$  = allowable shear stress for shaft material

STEP 3: Find length of key from

a.) Width of key, b= 
$$\frac{2M_t}{dl\tau_k}$$

 $\tau_k$  = allowable shear stress for key

b.) Thickness of key, 
$$h = \frac{4M_t}{dl\sigma_b}$$

Recommend the bigger one as length.

 $\sigma_{\text{b}}{}'$  = allowable crushing stress or bearing stress for key.

Procedure – Type 2: Length of key

**STEP 1**: Torque,  $M_t = 9.55 \times 10^6 \times P$ 

**STEP 2**: Diameter of shaft, d =  $\sqrt[3]{\frac{16M_t}{\pi \tau_s}}$ 

**STEP 3**: Design of Key

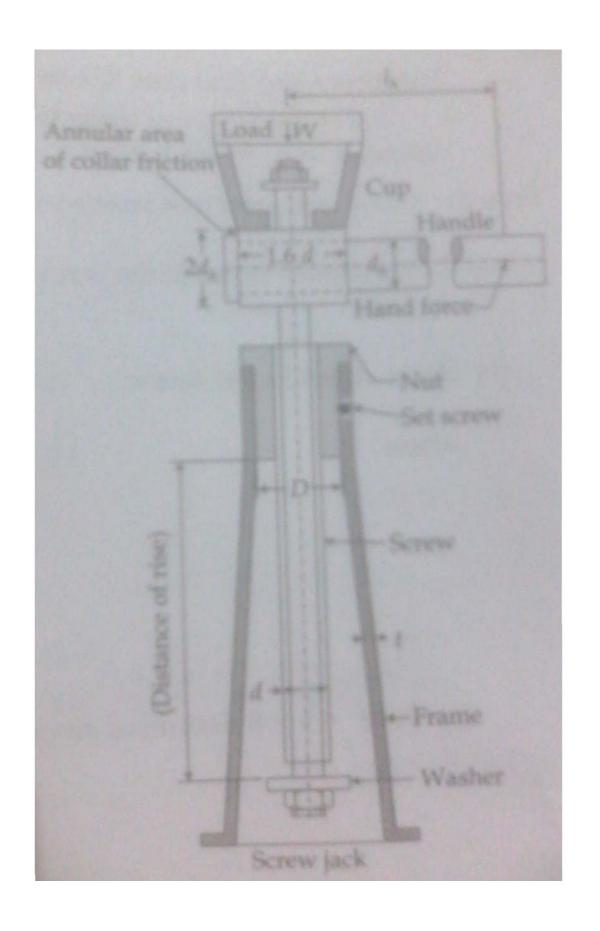
- a.) Length of key = length of hub = I
- b.) Width of key, b=  $\frac{2M_t}{dl\tau_k}$
- c.) Thickness of key,  $h = \frac{4M_t}{dl\sigma_b'}$

**AIM**- Design and drawing of Screw Jack

## **INTRODUCTION**

Screws used for power transmission are known as power screws. They provide a means for obtaining a large mechanical advantage, in such applications as screw jacks, c-lamps, hand presses land screw on lathe machines, hoisting machines etc.

## **SCREW JACK**



#### **NOTATIONS**

W = load to be lifted

d= outside diameter or nominal diameter of screw

p= pitch

 $d_h$  = diameter of handle

 $I_h$  = length of handle

D = outside diameter of nut

D<sub>i</sub>, D<sub>o</sub> = inside and outside the diameter of thrust collar

 $d_c$ = mean diameter of the thrust collar =  $D_i$  +  $D_o$ 

2

I<sub>n</sub>= nut length

t= thickness of body

 $\sigma_{\text{max}}\text{=}$  allowable normal stress in the screw

 $\tau_{\text{max}}\text{=}$  allowable shear stress in the screw

 $\sigma_{\text{b}}\text{=}$  allowable bending stress in the screw

 $\tau_n$ = allowable shear stress in the nut

 $\mu$  = coefficient of thread friction

 $\mu_{\text{c}}\text{=}$  coefficient of collar friction

## **Design Procedure**

# STEP 1: Design of screw

a.) Considering the screw under axial compression

$$\sigma_c = \frac{W}{A_c} = \infty$$
 core area,  $A_c = \frac{W}{A_c}$ 

 $\sigma_c$ = allowable compressive stress in screw =  $\sigma_{max}$ 

b.) Considering the screw as a column loaded in axial compression, when fully extended, Rankine' equation for columns

$$\sigma = W \left( 1 + a \left( \frac{I_e}{k} \right)^2 \right)$$

 $\sigma$  = allowable stress in the screw =  $\sigma_{max}$ 

$$A_c = \pi d_1^2/4$$

a= Rankine's Constant = 1/7500 for steels

I<sub>e</sub> = equivalent length of the column

Screw Jack is a columnwith one end fixed at nut and other end is free where the load is sitting.

So, Equivalent length, I<sub>e</sub>= 2 x (lift or extension)

## STEP 2: Check for principal stresses in the screw

a.) Compressive stress in the screw,  $\sigma_c$ =W

A

b.) Shear stress in the screw,  $\tau_s = M_{ts}r_1$ 

Where M<sub>ts</sub>= frictional torque in the screw only

$$= Wd_2 \left( \frac{\tan \alpha + \mu}{1 - \mu \tan \alpha} \right)$$

$$d_2 = d - \frac{1p}{2}$$
,  $\tan \alpha = \frac{1}{\pi d_2}$ 

(I= lead = 1xp assuming single start)

$$r_1 = \frac{d_1}{2}$$

$$J = \frac{\pi d_1^4}{32}$$

- c.) Combined or principal stresses
  - i. Maximum normal stress

$$\sigma_{\text{max}} = \frac{1}{2} \left\{ \sigma_c + \left[\sigma_c^2 + 4\tau_s^2\right]^{1/2} \right\}$$

ii. Maximum shear stress,  $\tau_{max} = \frac{1}{2} (\sigma_c^2 + 4\tau_s^2)^{1/2}$ 

# STEP 3: Design of screw head and collar

Assume pin head diameter, Do = 1.6d = outside the diameter of the collar

Pin diameter,  $D_i = 0.5d = Inside$  the diameter of the collar

So, Mean Diameter of the collar,  $d_c = D_i + D_o$ 

# STEP 4: Design of nut:

Assuming bronze for nut,

- a.) Length of nut,  $I_n = 4Wp$  $\sigma_b'\pi(d^2-d_1^2)$
- b.) Tensile stress in the nut =  $\sigma_{\text{nut}} = W$  $\pi/4(D^2-d^2)$ Assume,  $\sigma_{b}^{'} = 15MPa$  and  $\sigma_{nut}$  = 40 to 50MPa

**STEP 5:** Frictional torque

**STEP 5:** Frictional torque Total frictional torque including the collar friction 
$$M_t = W \left\{ \frac{d_2}{2} \left( \frac{\tan \alpha + \mu}{1 - \mu \tan \alpha} \right) + \frac{\mu_c d_c}{2} \right\}$$

STEP 6: Design of handle

- a.) Length of handle,  $I_h = M_t$
- b.) To find the diameter of handle, the handle is subjected to bending moment WKT  $M_b = \sigma_b$

Where  $M_b$ =bending moment =  $FI_h$ =  $M_t$ 

I = moment of inertia for handle, I = 
$$\pi d_h^4$$
64

 $C= d_h$ ,  $\sigma_b =$  allowable bending stress

**STEP 8:** Self locking condition

The screw jack to be of self locking type,

Hence check for self locking.

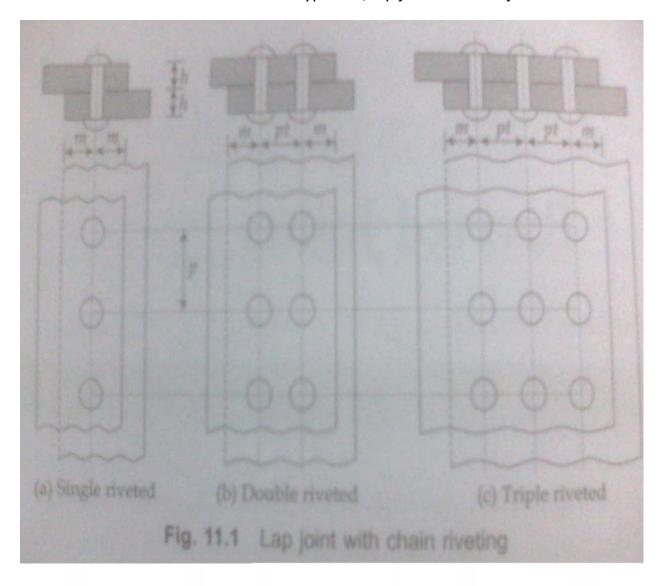
$$\frac{tan\alpha < \mu d_2 + \mu_c d_c}{d_2 - \mu \mu_c d_c}$$

**AIM**- Design and drawing of Riveted Joints

### **INTRODUCTION**

Two or more plates are joined by means of rivets and such joints are called riveted joints. These joints are permanent in nature unlike bolted joints. These are used in bridges, ships, boilers, tanks, etc.

Riveted Joints are classified into two types viz, lap joint and butt joint.



#### **NOTATIONS**

Pitch, p = It is the distance between centres of two consecutive rivets in a row

Margin, m = It is the distance from end of plate to first low of rivets.

Transverse pitch,  $p_t$  = Distance between two consecutive rows of rivets.

Diagonal pitch, $p_d$  = In zigzag riveting, the distance between centres of adjacent rivets inside by side rows

F = tensile or compressive load on plates

d= diameter of the rivet

d<sub>h</sub>= diameter of rivet hole

h = thickness of main plate

 $h_1, h_2$  = thickness of cover plates

 $i_1$  = number of rivets in single shear in one pitch length or repetitive length of joint

i<sub>2</sub> = number of rivets in double shear in one pitch length

C= Corrosion allowance 1 to 3mm

K = factor as per boiler code

∃ = efficiency

b = width of plate

 $\sigma_{t} \text{=} \ \sigma_{\theta} \text{=} \ \text{allowable tensile stress for plates}$ 

 $\tau$  = allowable shear stress for rivets

 $\sigma_c$ = allowable crushing stress for rivets

### **RIVETED JOINTS FOR BOILERS**

D<sub>1</sub>= Inside diameter of the boiler

P<sub>f</sub> = Fluid pressure or steam pressure

### **DESIGN PROCEDURE FOR BOILER JOINTS**

## **Part-I Longitudinal joint**

**Step 1:** Thickness of plate  $h = P_fD_i + C$ 

 $2 { ? } \sigma_\theta$ 

□ = Efficiency of joint = 0.7 to 0.8

C = Corrosion allowance = 1 to 3mm

**Step 2:** Diameter of the rivet,  $d = 6\sqrt{h}$ 

**Step 3:** Pitch of the rivets:

a.)  $p = \frac{(i_1 + 1.875i_2)\pi d^2\tau}{1.875i_2} + d_h$  and

 $4ph\sigma_{\theta}$ 

b.) p = Kh + 40

**Step 4:** Transverse pitch p<sub>t</sub> = 2.25d

**Step 5:** Margin m = 1.5d

**Step 6:** Thickness of cover plates:

- For equal covers  $h_1 = h_2 = 0.625h$
- For unequal covers  $h_1 = 0.625h$  and  $h_2 = 0.625h$

# **Step 7: Efficiency**

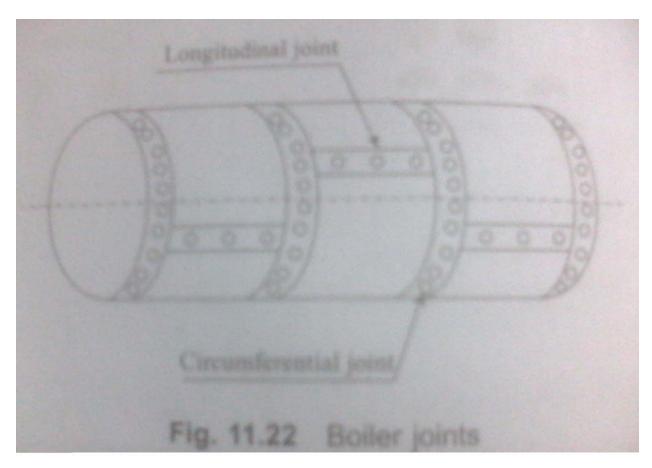
a.) Efficiency of plate,  $\eta_p = \frac{p-d}{P}$ 

b.) Efficiency of rivets in shear,  $\eta_{\tau} = \frac{i_1 + 1.875i_2 \pi d^2 \tau}{4ph\sigma_{\Theta}}$ 

**c.)** Efficiency of rivets in crushing, 
$$\eta_c = (i_2 + i_1 h_2) \sigma_c$$

h

$$h$$



# **PART-II Circumferential joints**

The plates to be riveted being same in both longitudinal and circumferential joints (h being same), the diameter of rivets, transverse pitch and margin are same.

h, d,  $p_t$  and m are same as above.

**Step 1:** Total steam load 
$$F = \left(\frac{\pi Di^2}{---}\right)^2$$

# **STEP 2:** Strength of each rivet

a.) In shear 
$$F_{\tau} = \frac{\pi d^2 \tau}{4}$$

b.) In crushing  $F_c = dh\sigma_c$ 

**STEP 3:** Number of rivets required = Steam Load

Minimum strength of rivet

**Step 4:** Rivets/Rows = i/row = Total number of rivets

Number of rows of rivets

Number of rows = 1 for single riveted joint

= 2 for double riveted joint

# **Step 5:** Pitch for circumferential joint

$$P_c = \frac{Circumference}{Rivets/Row} = \frac{\pi D_i}{i/row}$$

**Step 6:** Efficiency

a.) Efficiency of plate, 
$$\eta_p = \frac{p_c - d_h}{P_c}$$

b.) For rivets in shear, 
$$\eta_{\tau} = (i_1 + 1.875i_2)\pi d^2\tau$$

$$4ph\sigma_{\Theta}$$

c.) For rivets in crushing, 
$$\eta_c = \hat{i}_2 + i_1 h_2 \sigma_c$$

$$h \hat{i}_2 + i_1 h_2 \hat{\sigma}_c + \sigma_\theta$$